International Seminar on Applied Geometry in Andalusia

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Geometry Applied to DNA

We will survey the three main invariants involved in the doubly stranded DNA molecule. We will talk about linking L, twisting T and writhing W numbers and the fundamental result in the geometry of twisted, closed ribbon loops known as the Calugareanu theorem (also referred to as either White's formula or Calugareanu-White-Fuller theorem, which is expressed as $L = T + W4$.

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